

## Math 11U Trigonometric Identities

All of these identities use the reciprocal ratios, quotient identities, and/or the Pythagorean Identities.

1.  $\sin A \cot A = \cos A$

23.  $\frac{\sin A}{\csc A} + \frac{\cos A}{\sec A} = 1$

2.  $\cos A \tan A = \sin A$

24.  $\frac{\sec A}{\cos A} - \frac{\tan A}{\cot A} = 1$

3.  $\cot \theta \sec \theta = \csc \theta$

25.  $\sin^4 \theta - \cos^4 \theta = 2 \sin^2 \theta - 1$

4.  $\sin \theta \sec \theta = \tan \theta$

26.  $\sec^4 \theta - 1 = 2 \tan^2 \theta + \tan^4 \theta$

5.  $\cos A \csc A = \cot A$

27.  $\csc^4 A - 1 = 2 \cot^2 A + \cot^4 A$

6.  $\cot A \sec A \sin A = 1$

28.  $(\tan A \csc A)^2 - (\sin A \sec A)^2 = 1$

7.  $(1 - \cos^2 A) \csc^2 A = 1$

29.  $(\sec \theta \cot \theta)^2 - (\cos \theta \csc \theta)^2 = 1$

8.  $(1 - \sin^2 \theta) \sec^2 \theta = 1$

30.  $\tan^2 \theta - \cot^2 \theta = \sec^2 \theta - \csc^2 \theta$

9.  $\cot^2 \theta (1 - \cos^2 \theta) = \cos^2 \theta$

31.  $\frac{\sin A \cot^2 A}{\cos A} = \frac{1}{\tan A}$

10.  $(1 - \cos^2 A) \sec^2 A = \tan^2 A$

32.  $\frac{\sec^2 A \cot A}{\csc^2 A} = \tan A$

11.  $(1 + \tan^2 A) \cos^2 A = 1$

33.  $\sec \theta - \tan \theta \sin \theta = \cos \theta$

12.  $(\sec^2 A - 1) \cot^2 A = 1$

34.  $\tan \theta + \cot \theta = \sec \theta \csc \theta$

13.  $(1 - \cos^2 \theta)(1 + \tan^2 \theta) = \tan^2 \theta$

35.  $(\cos A + \sin A)^2 + (\cos A - \sin A)^2 = 2$

14.  $\sin^2 A (1 + \cot^2 A) = 1$

36.  $(1 + \tan \theta)^2 + (1 - \tan \theta)^2 = 2 \sec^2 \theta$

15.  $(\csc^2 \theta - 1) \tan^2 \theta = 1$

37.  $(\cot \theta - 1)^2 + (\cot \theta + 1)^2 = 2 \csc^2 \theta$

16.  $\sin^2 \theta \cot^2 \theta + \sin^2 \theta = 1$

38.  $\sin^2 \theta (1 - \cot \theta)^2 + \cos^2 \theta (1 + \tan \theta)^2 = 2$

17.  $(1 - \cos^2 A)(1 + \cot^2 A) = 1$

39.  $\cos^2 A (\sec^2 A - \tan^2 A) + \sin^2 A (\csc^2 A - \cot^2 A) = 1$

18.  $(1 + \tan^2 A)(1 - \sin^2 A) = 1$

40.  $\cot^2 A + \cot^4 A = \csc^4 A - \csc^2 A$

19.  $\sin^2 \theta \sec^2 \theta = \sec^2 \theta - 1$

41.  $\frac{\tan^2 \theta}{1 + \tan^2 \theta} \times \frac{1 + \cot^2 \theta}{\cot^2 \theta} = \sin^2 \theta \sec^2 \theta$

20.  $\csc^2 \theta \tan^2 \theta - 1 = \tan^2 \theta$

42.  $\frac{1}{1 - \sin \theta} + \frac{1}{1 + \sin \theta} = 2 \sec^2 \theta$

21.  $\frac{1}{\sec^2 A} + \frac{1}{\csc^2 A} = 1$

22.  $\frac{1}{\cos^2 \theta} - \frac{1}{\cot^2 \theta} = 1$

$$43. \frac{\tan A}{\sec A - 1} + \frac{\tan A}{\sec A + 1} = 2 \csc A$$

$$44. \frac{1}{1+\sin^2 A} + \frac{1}{1+\csc^2 A} = 1$$

$$45. (\sec \theta + \csc \theta)(\sin \theta + \cos \theta) = \sec \theta \csc \theta + 2$$

$$46. (\cos \theta - \sin \theta)(\csc \theta - \sec \theta) = \sec \theta \csc \theta - 2$$

$$47. (1 + \cot A + \csc A)(1 + \cot A - \csc A) = 2 \cot A$$

$$48. (\sec A + \tan A - 1)(\sec A - \tan A + 1) = 2 \tan A$$

$$49. (\sin A + \csc A)^2 + (\cos A + \sec A)^2 = \tan^2 A + \cot^2 A + 7$$

$$50. (\tan \theta + \sec \theta)^2 = \frac{1+\sin \theta}{1-\sin \theta}$$

$$51. \sin^4 \theta + 2 \cos^2 \theta - \cos^4 \theta = 1$$

$$52. (1 + \tan^2 A)(1 - \tan^2 A) = 2 \sec^2 A - \sec^4 A$$

$$53. \cos^3 A + \sin^3 A = (\cos A + \sin A)(1 - \sin A \cos A)$$

$$54. \sin^4 \theta - 2 \sin^2 \theta = \cos^4 \theta - 1$$

$$55. \frac{\sqrt{1-\cos^2 \theta}}{\cos \theta} \times \sqrt{\sec^2 \theta - 1} = \tan^2 \theta$$

$$56. \frac{\cos A}{1+\sin A} + \frac{1+\sin A}{\cos A} = 2 \sec A$$

$$57. \sin^2 A \tan A + \cos^2 A \cot A + 2 \sin A \cos A = \tan A + \cot A$$